

MAT180 HW04

(ADD NAME)

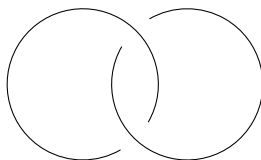
Due 4/29/23 at 11:59 pm on Gradescope

Reminder Your homework submission must be typed up in full sentences, with proper mathematical formatting. The following resources may be useful as you learn to use TeX and Overleaf:

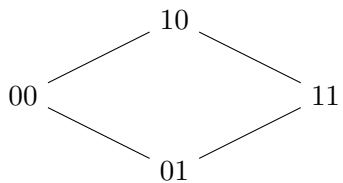
- Overleaf's introduction to LaTeX:
https://www.overleaf.com/learn/latex/Learn_LaTeX_in_30_minutes
- Detexify:
<https://detexify.kirelabs.org/classify.html>

Exercise 1

Let H denote the following diagram of the (unoriented) Hopf link:



- (a) Draw the *cube of resolutions* for the diagram above. That is, replace the binary strings below with the associated smoothings of the diagram:



Remark. The cube of resolutions can be viewed as a graph representing the partially ordered set $\{0, 1\}^n$ where the bit string $a = a_1a_2 \dots a_n \leq b_1b_2 \dots b_n$ iff for each i , $a_i \leq b_i$.

- (b) Compute the Kauffman bracket polynomial $\langle H \rangle$.
- (c) Use your computation of $\langle H \rangle$ to compute the Jones polynomials of the positively linked Hopf link H^+ and the negatively linked H^- in terms of the variable q .